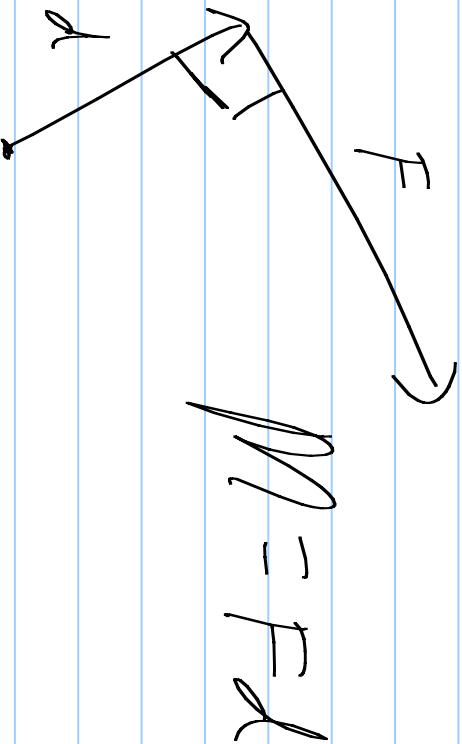


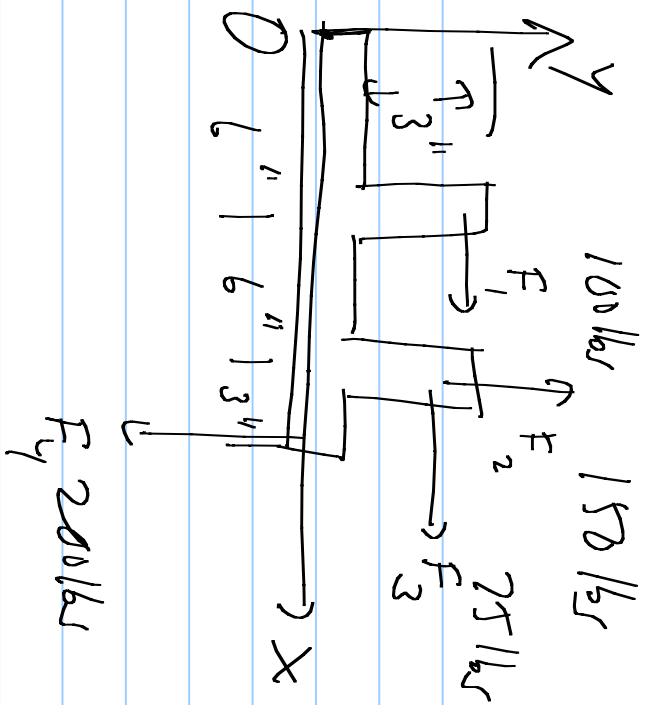
EGR 180 6/8

Moments

Force times a distance

Force & distance are perpendicular



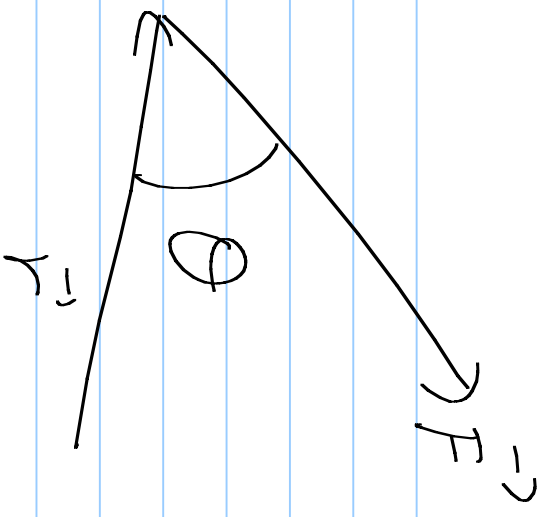


$$M_1 = 3 \cdot 100 = 308 \text{ in}\cdot\text{lb}$$

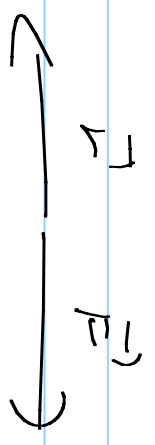
$$M_2 = 12 \cdot 150 = 1800 \text{ in}\cdot\text{lb}$$

$$M_3 = 3 \cdot 25 = 75 \text{ in}\cdot\text{lb}$$

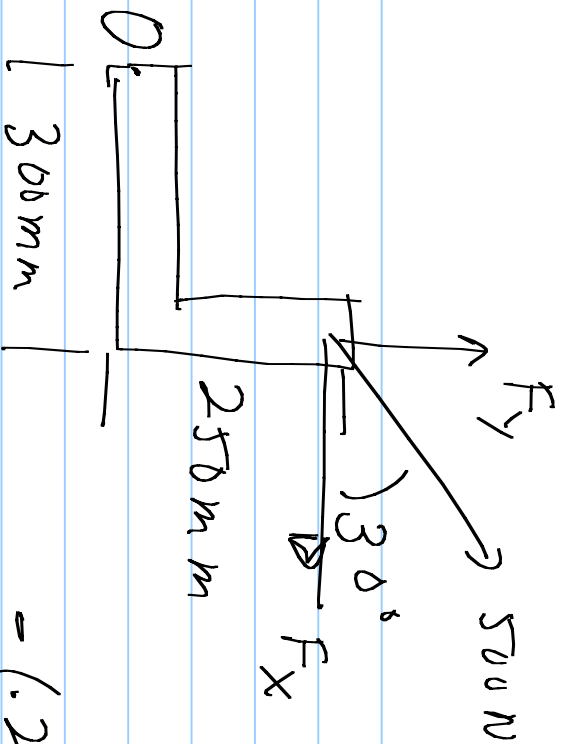
$$M_y = 15 \cdot 200 = 3000 \text{ in}\cdot\text{lb}$$



$$M = |\vec{F}| |\vec{r}| \sin \theta$$



$$M = r F \sin \theta$$



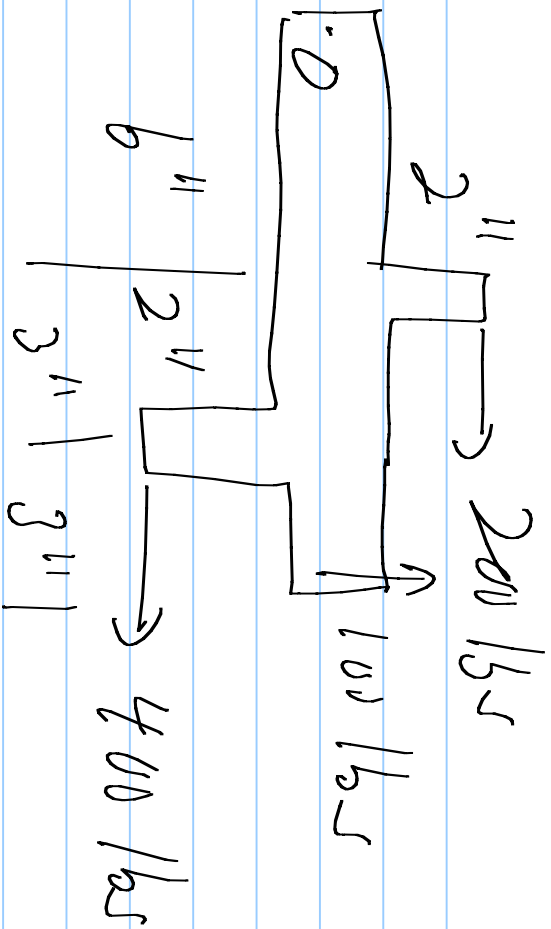
$$M = \sum m_i$$

$$= (-.25) 500 \cos(30) = -108.3 \text{ N}\cdot\text{m}$$

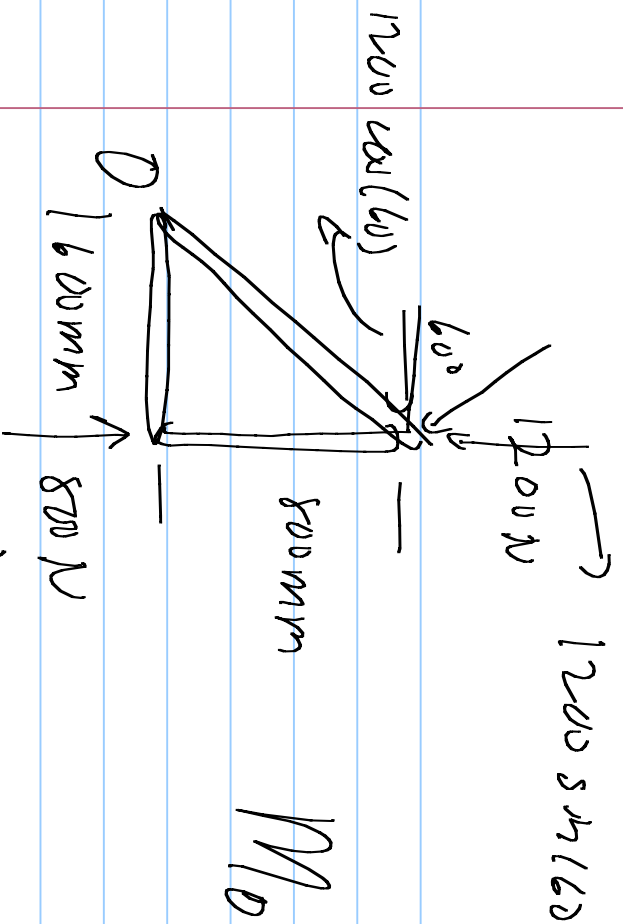
$$(-.3) (500 \sin(30)) = 75.0 \text{ N}\cdot\text{m}$$

$$= \underline{\underline{-33.3 \text{ N}\cdot\text{m}}}$$

Moments are free vectors

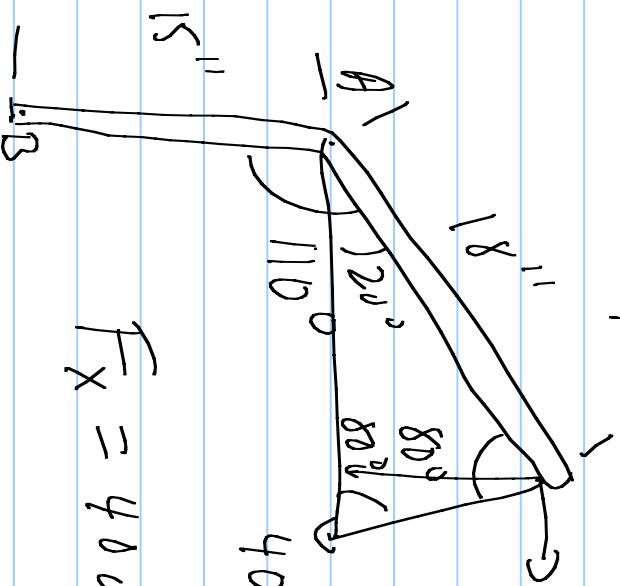


$$\begin{aligned}
 M_0 &= -2 \cdot 200 + 2 \cdot 400 + 12 \cdot 100 \\
 &= -400 + 800 + 1200 = 1600 \text{ in. lbs}
 \end{aligned}$$



$$M_D = (.6)(800) - (.6)(1639.2)$$

$$= (.8)(600) = -623.5 \text{ N}\cdot\text{m}$$



$$M_A = -18 \cdot 40 \cdot \sin(80^\circ) = -709.1 \text{ in}\cdot\text{lb}$$

$$M_B = -18 \cos(20) \cdot 40 \sin(80) \\ = (15 + 18 \sin(20)) \cdot 40 \cos(80)$$

$$F_x = 40 \cos(80) \quad F_y = 40 \sin(80) = -813.3 \text{ in}\cdot\text{lb}$$

Vector Moments

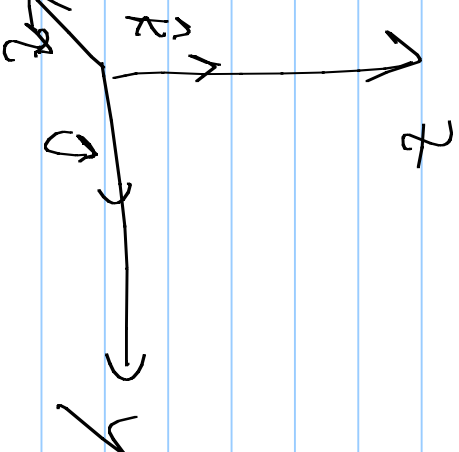
$$\vec{M} = \vec{r} \times \vec{F}$$

$$\hat{i} \times \hat{j} = \hat{k} \quad \hat{j} \times \hat{i} = -\hat{k}$$

$$\hat{j} \times \hat{k} = \hat{i} \quad \hat{k} \times \hat{j} = -\hat{i}$$

$$\hat{k} \times \hat{i} = \hat{j} \quad \hat{i} \times \hat{k} = -\hat{j}$$

$$\vec{u} \times \vec{v} = -\vec{v} \times \vec{u}$$



$$M = |\vec{r}| |\vec{F}| \sin(\theta)$$

\vec{u}

$$\vec{u} = u_x \vec{i} + u_y \vec{j} + u_z \vec{k}$$

$$\vec{v} = v_x \vec{i} + v_y \vec{j} + v_z \vec{k}$$

$$\vec{u} \times \vec{v} = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ u_x & u_y & u_z \\ v_x & v_y & v_z \end{vmatrix}$$

$$= \vec{i} (u_y v_z - v_y u_z)$$

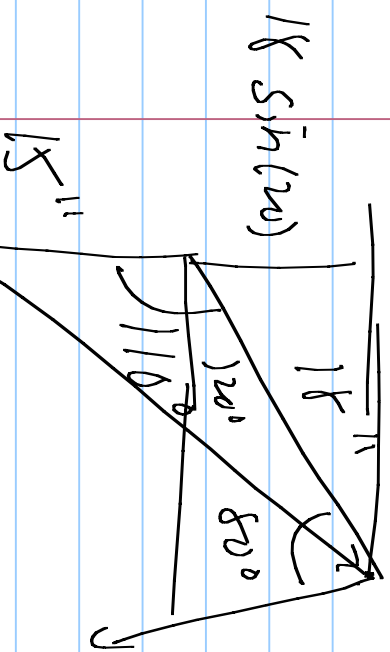
$$- \vec{j} (u_x v_z - v_x u_z)$$

$$+ \vec{k} (u_x v_y - v_x u_y)$$

$$\vec{w} = 2\vec{i} + 3\vec{j} - 4\vec{k}$$

$$\vec{v} = 4\vec{i} - 2\vec{j} + 2\vec{k}$$

$$\vec{w} \times \vec{v} = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 2 & 3 & -4 \\ 4 & -2 & 2 \end{vmatrix} = -\vec{j}(4+16) \\ + \vec{k}(-4-12) \\ = -20\vec{j} - 16\vec{k}$$



$$\vec{r} = 18 \cos 20 \hat{i} + 18 \sin 20 \hat{j}$$

$$\vec{F} = 40 \cos 80 \hat{i} - 40 \sin 80 \hat{j}$$

40 lbs

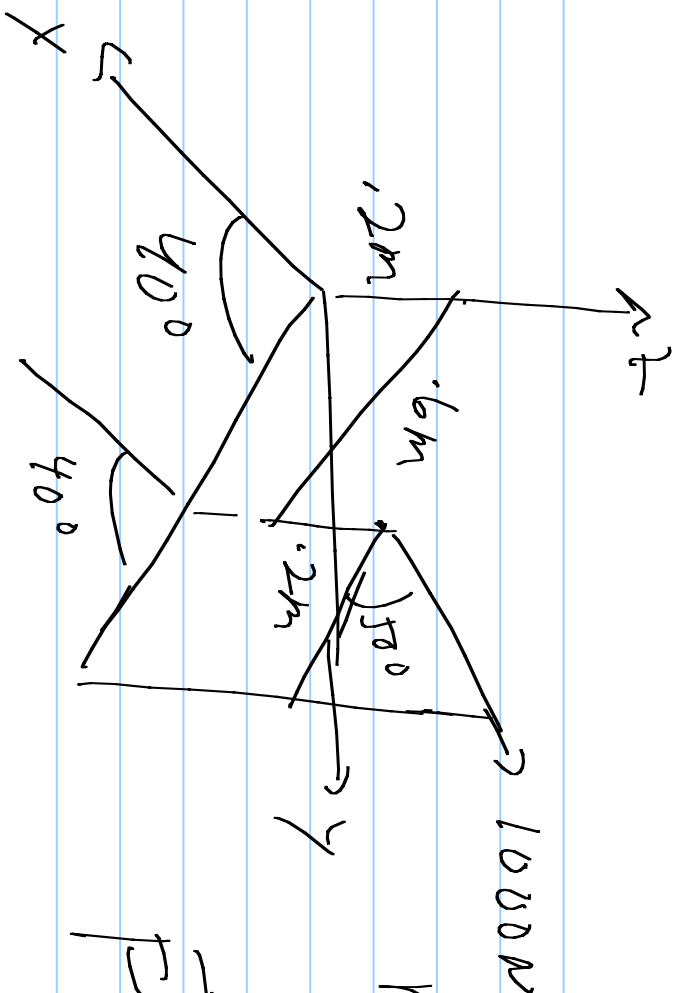
$$\vec{M} = \vec{r} \times \vec{F} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 18 \cos 20 & 18 \sin 20 & 0 \\ 40 \cos 80 & -40 \sin 80 & 0 \end{vmatrix}$$

$$\begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 18 \cos 20 & 18 \sin 20 & 0 \\ 40 \cos 80 & -40 \sin 80 & 0 \end{vmatrix}$$

$$= \hat{k} (-40 \cdot 18 \cos 20 \sin 80) - 48 \cos 80$$

$$= -813.3 \hat{k} \text{ in. lbs}$$

(15 + 18 sin 20)



$$\vec{r} = 0.6 \cos(40^\circ) \hat{i} + 0.6 \sin(40^\circ) \hat{j} + 0.2 \hat{k}$$

$$\vec{F} = 1000 \cos(50^\circ) \cos(40^\circ) \hat{i} + 1000 \cos(50^\circ) \sin(40^\circ) \hat{j} + 1000 \sin(50^\circ) \hat{k}$$

$$\vec{M} = \vec{r} \times \vec{F} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 0.46 & 0.386 & 0.2 \\ 492.4 & 413.2 & 766.0 \end{vmatrix} = \hat{i} (130.2) - \hat{j} (155.1) + \hat{k} (0) \text{ N}\cdot\text{m}$$